



# The new understanding on photocatalytic mechanism of visible-light response N–S codoped anatase TiO<sub>2</sub> by first-principles

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## ABSTRACT

The geometry structure, formation energy and electronic property of N–S codoped anatase TiO<sub>2</sub> (NS–TiO<sub>2</sub>) were investigated by the density functional theory (DFT) of first-principles. The result indicated that the O-poor growth condition is beneficial to the formation of NS–TiO<sub>2</sub> except the N<sub>Ti</sub>S<sub>Ti</sub>–TiO<sub>2</sub> with non-sensitivity to the atmosphere. The visible-light photocatalytic activity of NS–TiO<sub>2</sub> was influenced by many factors including the value of energy gap ( $E_g$ ), the distribution of impurity level, the property of impurity level, the location of Fermi level and the energy in the edges of band gap. The impurity level localized in the top of valence band reduced the energy gap, leading to the absorption of visible light. Besides, the impurity level delocalized in the band gap reduced the critical energy of available photon, which further strengthened the absorption of visible light. Moreover, the bent impurity level was the efficient separation center of photogenerated electron and hole, while the flat impurity level was the combination center of photogenerated electron and hole. Further, the valence band and conduction band of NS–TiO<sub>2</sub> moved toward the low energy region (down shift), resulting in the stronger oxidizability of photogenerated hole in the top of valence band and weaker reducibility of photogenerated electron in the bottom of conduction band. This indicated that the dominant oxidant species during photocatalytic reaction for NS–TiO<sub>2</sub> was hole and •OH radical instead of •O<sub>2</sub><sup>−</sup> ion.

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## 1. Introduction

Since the photocatalytic H<sub>2</sub> production by splitting water on TiO<sub>2</sub> electrodes was reported in 1972 [1], semiconductor photocatalytic materials and technology have been widely investigated for the potential application in degradation of pollutant, photosynthesis of organic compounds and production of hydrogen [2–12]. Due to the chemical inertness, strong oxidizing power, nontoxicity, long-term stability and low cost, TiO<sub>2</sub> has been proven to be the most suitable photocatalytic material in hydrogen generation and environmental remediation among various oxide and nonoxide semiconductor photocatalysts [13,14]. However, with a large intrinsic band gap (3.2 eV for anatase and 3.0 eV for rutile), TiO<sub>2</sub> only can absorb the ultraviolet (UV) light which is a small portion of solar spectrum (containing about 4% ultraviolet light and 43% visible light) [15,16]. As a result, the effective utilization of visible light becomes a hot research topic. Many methods, including doping impurity atoms (B, C, N, F, P, S, Ni, etc.) [17–25] and

sensitizing TiO<sub>2</sub> with organic dyes or narrow-gap semiconductor quantum dots (CdS, CdSe, InP, PbS, etc.) [26–31], have been developed to reduce the energy gap of TiO<sub>2</sub>. As for the doping approaches, a large number of N-doped anatase TiO<sub>2</sub> (N–TiO<sub>2</sub>) and S-doped anatase TiO<sub>2</sub> (S–TiO<sub>2</sub>) have been synthesized, which shifts the absorption edge of TiO<sub>2</sub> into the visible region [32–40]. The corresponding theoretical study also has been performed to discuss the origination of absorption of visible light. Many literatures indicate that the band gap of doped TiO<sub>2</sub> is narrowed. But other literatures suggest that the impurity state in the band gap acts as the ladder for transferring electron, which reduces the maximum energy gap in the band gap [41–45]. Furthermore, the NS–TiO<sub>2</sub> is also prepared, indicating that NS–TiO<sub>2</sub> has higher visible-light photocatalytic activity than N–TiO<sub>2</sub> and S–TiO<sub>2</sub> [46–52]. But about the existing forms of N and S atom are often debated. Also, there is still no certain answer. Very recently, our group also synthesized the NS–TiO<sub>2</sub> [53], indicating that various defects induced by the impurity atoms exist in the doped TiO<sub>2</sub>.

Herein, for the first time, we systematically investigate the geometry structure, formation energy and electronic property of NS–TiO<sub>2</sub>. The stable NS–TiO<sub>2</sub> is determined by comparing the formation energy of doping process. The originations of enhanced visible-light photocatalytic activity are investigated by the value

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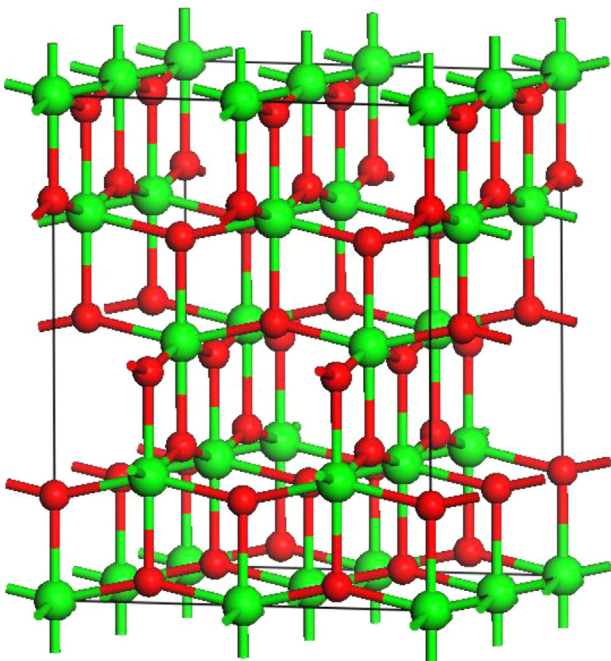
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of energy gap, the distribution of the impurity state, the property of impurity state, the location of Fermi level and the energy value in the edges of band gap. This study will provide new insight into understanding the mechanism of enhanced visible-light photocatalytic activity for the NS–TiO<sub>2</sub> and designing new photocatalytic materials with required electronic property.

## 2. Computational details

All DFT calculations were performed with CASTEP package based on the plane-wave-pseudo-potential approach [54]. Considering the advantage of the generalized gradient approximation (GGA) in dealing with the electron gas of solid constituted of light atoms, the exchange–correlation function adopted the Perdew–Burke–Ernzerhof (PBE) of GGA [55,56]. The ultrasoft pseudo-potential was used to describe the interaction between valence electrons and the ionic core. The 2 × 2 × 1 supercell (containing 16 Ti atoms and 32 O atoms, see Fig. 1) of anatase TiO<sub>2</sub> was simultaneously doped with one N atom and one S atom. The two impurity atoms were introduced into the supercell by the modes of N<sub>O</sub> (N atom substituting lattice O atom), N<sub>Ti</sub> (N atom substituting lattice Ti atom), N<sub>i</sub> (N atom occupying the interstitial position), S<sub>O</sub> (S atom substituting lattice O atom), S<sub>Ti</sub> (S atom substituting lattice Ti atom) and S<sub>i</sub> (S atom occupying the interstitial position), resulting in nine different kinds of N–S codoped anatase TiO<sub>2</sub> models. In addition, we kept the largest distance between the two impurity atoms as soon as possible to distribute the impurity atoms in the supercell. The doping concentrations (mole ratio) of the N and S atoms both changed from 2.08% (existing two substitutional atoms) to 2.00% (existing two interstitial atoms), similar to those obtained from some experiments [12,13]. The cut-off energy of 400 eV, the Monkhorst–Pack k-point mesh of 4 × 4 × 4 and the self-consistent field of 5 × 10<sup>−5</sup> eV/atom were used to perform geometry optimizations [57]. The optimized calculation was carried out until the energy, max force, max stress and max displacement were less than 2.0 × 10<sup>−5</sup> eV/atom, 0.05 eV/Å, 0.1 GPa and 0.002 Å, respectively. Besides, the accuracy of the calculations



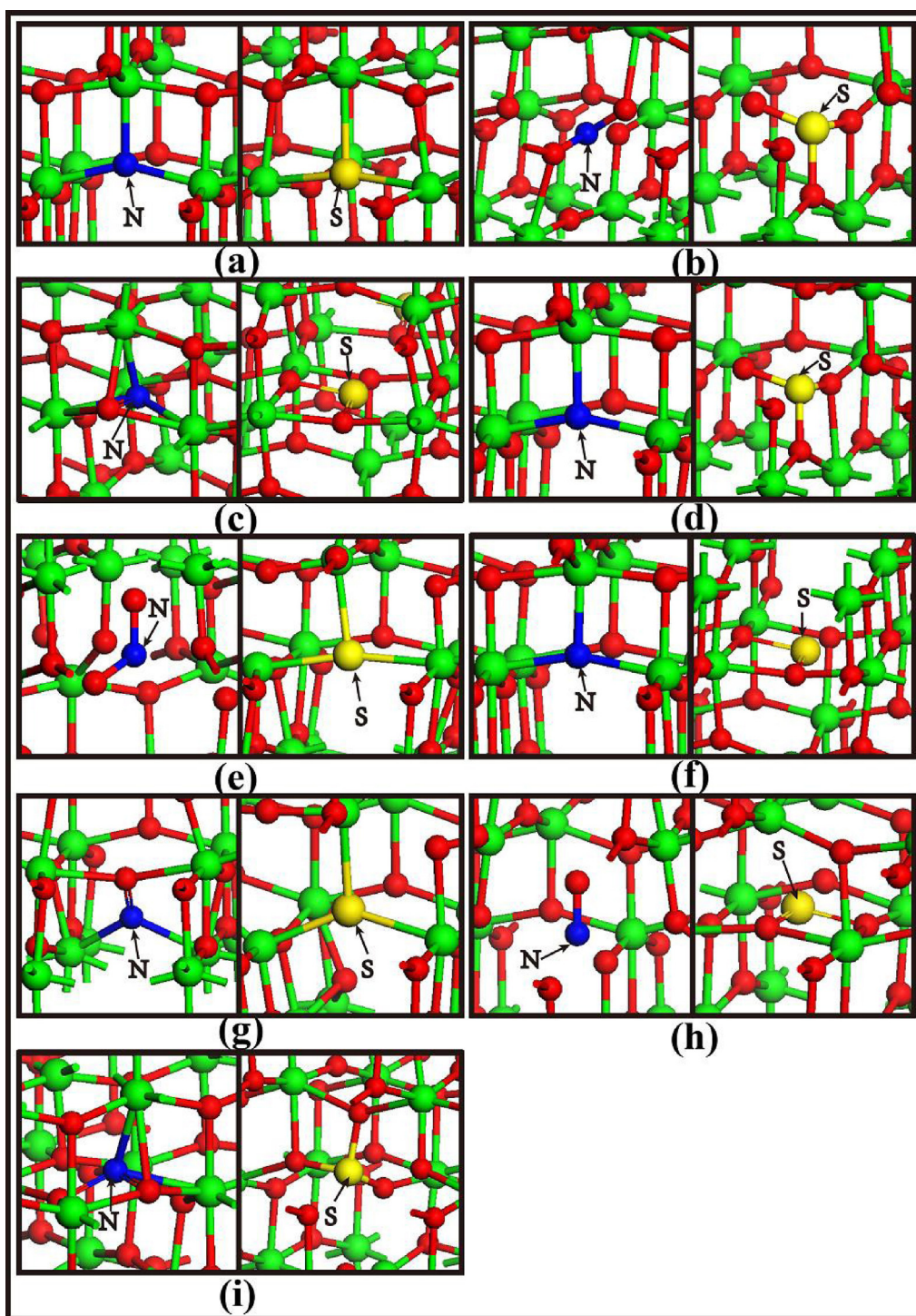
**Fig. 1.** The geometry structures for 2 × 2 × 1 supercell of anatase TiO<sub>2</sub>. The big green sphere represents Ti atom and the small red sphere represent O atom (For interpretation of the references to color in this figure legend, the reader is referred to the web version of the article.).

was tested by improving the cutoff energy and the number of k point, the results of which showed that the energy and geometry structure almost did not changed. After the geometry optimization was finished, the band structure and projected density of state (PDOS) of NS–TiO<sub>2</sub> were calculated. Furthermore, to compare the electronic properties of NS–TiO<sub>2</sub> with those of single-doped TiO<sub>2</sub> (N–TiO<sub>2</sub> and S–TiO<sub>2</sub>), the supercell models of N<sub>O</sub>–TiO<sub>2</sub>, N<sub>Ti</sub>–TiO<sub>2</sub>, N<sub>i</sub>–TiO<sub>2</sub>, S<sub>O</sub>–TiO<sub>2</sub>, S<sub>Ti</sub>–TiO<sub>2</sub> and S<sub>i</sub>–TiO<sub>2</sub> were also calculated.

**Table 1**  
Optimized cell parameters and bond lengths for N–S codoped anatase TiO<sub>2</sub>.

No.	Doped TiO <sub>2</sub> <sup>a</sup>	Structure parameter (Å)				Bond length (Å)			
		<i>a</i>	<i>b</i>	<i>c</i>	N–O	N–Ti	S–O	S–Ti	
(a)	N <sub>O</sub> S <sub>O</sub>	3.805	3.879	9.766		1.895 <sub>eq</sub> (2) <sup>b</sup> 1.917 <sub>ax</sub>			2.226 <sub>eq</sub> (2) 2.430 <sub>ax</sub>
(b)	N <sub>Ti</sub> S <sub>Ti</sub>	3.842	3.791	9.919	1.291 <sub>eq</sub> 1.282 <sub>ax</sub>		1.489 <sub>eq</sub> 1.523 <sub>eq</sub> 1.570 <sub>ax</sub>		
(c)	N <sub>i</sub> S <sub>i</sub>	3.871	3.844	9.715	1.458	2.035 <sub>eq</sub> 2.049 <sub>eq</sub> 2.063 <sub>ax</sub>	1.695 1.714		
(d)	N <sub>O</sub> S <sub>Ti</sub>	3.862	3.786	9.761		1.875 <sub>eq</sub> 1.902 <sub>eq</sub> 1.933 <sub>ax</sub>	1.504 <sub>eq</sub> 1.526 <sub>eq</sub> 1.566 <sub>ax</sub>		
(e)	N <sub>Ti</sub> S <sub>O</sub>	3.744	3.983	10.071	1.255 <sub>eq</sub> 1.284 <sub>ax</sub>				2.299 <sub>eq</sub> 2.339 <sub>eq</sub> 2.382 <sub>ax</sub>
(f)	N <sub>O</sub> S <sub>i</sub>	3.879	3.841	9.657		1.933 <sub>eq</sub> 1.922 <sub>eq</sub> 1.884 <sub>ax</sub>	1.696 1.709		
(g)	N <sub>i</sub> S <sub>O</sub>	3.813	3.806	10.155	1.319	2.057 2.060			2.236 <sub>eq</sub> 2.334 <sub>eq</sub> 2.362 <sub>ax</sub>
(h)	N <sub>Ti</sub> S <sub>i</sub>	3.915	3.821	9.962	1.221		1.638 1.680		
(i)	N <sub>i</sub> S <sub>Ti</sub>	3.851	3.818	9.842	1.464 1.449	2.247 <sub>eq</sub> 2.159 <sub>ax</sub>	1.595 <sub>eq</sub> 1.534 <sub>eq</sub> 1.616 <sub>ax</sub>		

<sup>a</sup> In pure anatase TiO<sub>2</sub>: *a* = *b* = 3.807 Å, *c* = 9.667 Å, equatorial Ti–O = 1.947 Å and axial Ti–O = 2.005 Å.  
<sup>b</sup> The number in the parentheses shows the number of bonds with same length.



**Fig. 2.** The partial geometry structures for optimized N–S codoped anatase  $\text{TiO}_2$  supercells: (a)  $\text{N}_0\text{S}_0\text{--TiO}_2$ , (b)  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}\text{--TiO}_2$ , (c)  $\text{N}_i\text{S}_i\text{--TiO}_2$ , (d)  $\text{N}_0\text{S}_{\text{Ti}}\text{--TiO}_2$ , (e)  $\text{N}_{\text{Ti}}\text{S}_0\text{--TiO}_2$ , (f)  $\text{N}_0\text{S}_i\text{--TiO}_2$ , (g)  $\text{N}_i\text{S}_0\text{--TiO}_2$ , (h)  $\text{N}_{\text{Ti}}\text{S}_i\text{--TiO}_2$ , (i)  $\text{N}_i\text{S}_{\text{Ti}}\text{--TiO}_2$ . The green spheres stand for Ti atoms, the red spheres for O atoms, the blue spheres for N atoms, and the yellow spheres for S atoms (For interpretation of the references to color in this figure legend, the reader is referred to the web version of the article.).

### 3. Results and discussion

#### 3.1. Optimized structures

In this work, the NS– $\text{TiO}_2$  was investigated. The partial geometry structures from the optimized supercells of NS– $\text{TiO}_2$  are shown in Fig. 2. It is clear that the  $\text{N}_0$  and  $\text{S}_0$  atoms in the doped  $\text{TiO}_2$  (see Fig. 2a, d, e, f and g) all keep the initial coordination number of O atom, but the difference is that the lengths of Ti–S bonds

(more than 2.2 Å, see Table 1) are larger than those of Ti–N bonds (less than 1.95 Å) and Ti–O bonds (1.947<sub>eq</sub> and 2.005<sub>ax</sub> Å) in pure anatase  $\text{TiO}_2$ . This is due to the larger radius of S atoms than those of N and O atoms. As a result, the structure parameters along with the direction of Ti–S bonds extend for a little. Because Ti– $\text{N}_0$  bonds are shorter than Ti–O bonds in pure  $\text{TiO}_2$ , the structure parameters along with the direction of Ti– $\text{N}_0$  bonds decrease. For the impurity atoms substitutional to Ti atoms, the  $\text{N}_{\text{Ti}}$  and  $\text{S}_{\text{Ti}}$  atoms cannot maintain same high coordination number with Ti atom, due to the



relatively simpler electronic orbits of N and S atoms than that of Ti atom. Thus the coordination numbers of the  $N_{Ti}$  and  $S_{Ti}$  atoms in the doped  $TiO_2$  (see Fig. 2b, d, e, h and i) are smaller than that of Ti atom in pure  $TiO_2$ . Especially, the  $N_{Ti}$  atom in  $N_{Ti}S_{O_i}-TiO_2$  forms the approximate  $NO_2$  molecule (see Fig. 2e). However, the  $N_{Ti}$  atom in the  $N_{Ti}S_{Ti}-TiO_2$  forms the approximate  $NO$  molecule (see Fig. 2h). This has been confirmed by the experiment [47]. But the  $S_{Ti}$  atoms in  $N_{O_i}S_{Ti}-TiO_2$ ,  $N_{Ti}S_{Ti}-TiO_2$  and  $N_iS_{Ti}-TiO_2$  (see Fig. 2b, d and i) all are bonded to two equatorial O atoms and one axial O atom constituting the structures of  $SO_3$  tetrahedron, which is confirmed by the XPS investigation [46]. Besides, the considerable modification of coordination number seriously changes the local lattice structure, resulting in the lattice distortion and the variation of cell parameter. For the impurity atoms in the interstitial position, the  $N_i$  atoms in the  $N_iS_{Ti}-TiO_2$ ,  $N_iS_{O_i}-TiO_2$  and  $N_iS_{Ti}-TiO_2$  (see Fig. 2c, f and i) exhibit complex coordination modes. The  $N_i$  atoms are simultaneously bonded to the O and Ti atoms. However, the  $S_i$  atoms in  $N_iS_{Ti}-TiO_2$ ,  $N_{O_i}S_{Ti}-TiO_2$  and  $N_{Ti}S_{Ti}-TiO_2$  (see Fig. 2c, f and h) all are only bonded to two adjacent O atoms. Though the introduced interstitial atoms form some new  $N_i-O$  (ranging from 1.319 to 1.464 Å) and  $S_i-O$  (ranging from 1.638 to 1.714 Å) bonds which are longer than the corresponding  $N_{Ti}-O$  (ranging from 1.221 to 1.291 Å) and  $S_{Ti}-O$  (ranging from 1.489 to 1.616 Å) bonds, the coordination numbers of most matrix atoms are not modified, implying little lattice deformation. Therefore, compared to the  $N_{Ti}$  and  $S_{Ti}$  atoms, the  $N_i$  and  $S_i$  atoms generates the smaller change in lattice structure. It should be noted that the coordination modes of  $N_{Ti}$  and  $N_i$  atoms vary with the location of S atom ( $S_{O_i}$ ,  $S_{Ti}$  and  $S_i$ ) though the N and S atoms are not directly bonded to each other, implying the indirect interaction existing between N and S atoms. But the coordination modes of  $S_{O_i}$ ,  $S_{Ti}$  and  $S_i$  atoms are not influenced by the N atom, considered from the larger atom radius and weaker mobility of S atom than those of N atom.

### 3.2. Formation energies

The analysis on optimized geometry structure shows that the different doping ways generate different lattice distortions, which makes the supercells of NS- $TiO_2$  with various total energies. Therefore, to compare the relative feasibilities of doping ways above, the formation energies ( $E_{form}$ ) of NS- $TiO_2$  supercells were investigated. The  $E_{form}$  is calculated by following formula:

$$E_{form} = E_{doped} - E_{pure} - \mu_N - \mu_S + x\mu_O + y\mu_{Ti} \quad (1)$$

where  $E_{doped}$  is the total energy of NS- $TiO_2$  supercell and  $E_{pure}$  is the total energy of the pure  $TiO_2$  supercell [58,59].  $\mu_N$ ,  $\mu_S$ ,  $\mu_O$  and  $\mu_{Ti}$  are the chemical potentials of N, S, O and Ti atoms, respectively. The coefficients  $x$  and  $y$  (equal to 0, 1 or 2) represent the numbers of O and Ti atoms substituted by impurity atoms, respectively. It should be mentioned that  $E_{form}$  is not fixed but depends on the growth condition. By adjusting the  $O_2$  pressure, the growth condition can be changed from O-rich to Ti-rich (O-poor). The relationships between  $\mu_O$  and the chemical potentials of N, S and Ti atoms are as follows:

$$2\mu_O + \mu_N = \mu(NO_2) \quad (2)$$

$$2\mu_O + \mu_S = \mu(SO_2) \quad (3)$$

$$2\mu_O + \mu_{Ti} = \mu(TiO_2) \quad (4)$$

Under O-rich growth condition,  $\mu_O$  is determined by the ground-state energy of the  $O_2$  molecule ( $\mu_O = \mu(O_2)/2$ ). Thus the chemical potentials of N, S and Ti atoms can be obtained from the formulae (2)–(4), respectively. Under O-poor growth condition,  $\mu_{Ti}$  is determined by the ground-state energy of bulk Ti ( $\mu_{Ti} = \mu_{bulk}/n$ ,  $n$  is the number of Ti atom in the bulk Ti). According to the formula (4),

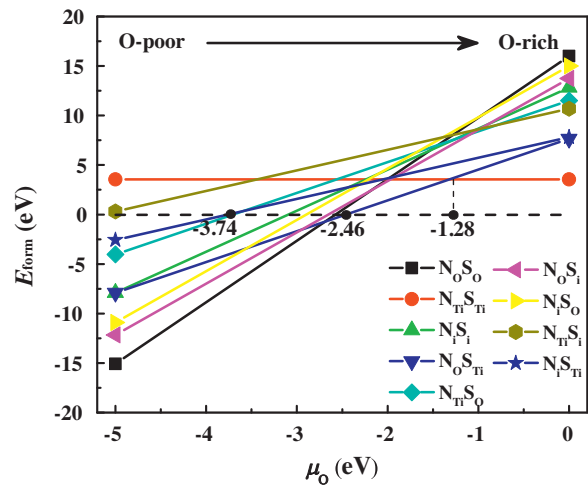


Fig. 3. Formation energies (eV) for the N–S codoped anatase  $TiO_2$ .

$\mu_O$  is calculated. Then  $\mu_N$  and  $\mu_S$  can be obtained from the formulae (2) and (3), respectively. Considering that the calculated  $\mu_O$  in O-rich growth condition are more 5 eV than that in O-poor growth condition,  $\mu_O$  is transformed into the form of  $\mu_O = \mu(O_2)/2 + \mu'_O$ , where  $\mu'_O = -5$  eV corresponds to O-poor growth condition and  $\mu'_O = 0$  eV corresponds to the O-rich growth condition (condensation oxygen). According to the formulae (1)–(4),  $E_{form}$  are calculated from the following formula:

$$E_{form} = E_{doped} - E_{pure} - \mu(NO_2) - \mu(SO_2) + \times (2 + x/2 - y) \times \mu(O_2) + y\mu(TiO_2) + (4 + x - 2y) \times \mu'_O \quad (5)$$

Consequently, the  $E_{form}$  of NS- $TiO_2$  can be regarded as the linear function of  $\mu'_O$ . The  $\mu'_O$  can range from  $-5$  to  $0$  eV. Fig. 3 exhibits the functional relationship between  $E_{form}$  and  $\mu'_O$  for the nine different kinds of NS- $TiO_2$ . It can be clearly seen that the  $E_{form}$  of  $N_{Ti}S_{Ti}-TiO_2$  does not change with  $\mu'_O$ , while the  $E_{form}$  of other NS- $TiO_2$  increase with  $\mu'_O$  rising. It is obvious that the  $N_{Ti}S_{Ti}-TiO_2$  is not sensitive to the outside atmosphere. However, the O-poor condition supports the formation of other NS- $TiO_2$  (anaerobic NS- $TiO_2$ ). Especially, the  $N_{O_i}S_{O_i}-TiO_2$  has the lowest  $E_{form}$  under the O-poor condition. Besides, the  $E_{form}$  of  $N_{O_i}S_{Ti}-TiO_2$  and  $N_iS_{O_i}-TiO_2$  are lower than  $-10$  eV. This confirms that the N and S atoms prefer to substitute O atom or occupy the interstice of lattice under the O-poor condition. The previous analysis on geometry structure verifies that the N-Ti-O, N-O-Ti, S-Ti-O and S-O-Ti linkages exist in the  $N_{O_i}S_{O_i}-TiO_2$ ,  $N_{O_i}S_{Ti}-TiO_2$  and  $N_iS_{O_i}-TiO_2$ , which are consistent with many experiments [46,48,50,53]. As the  $\mu'_O$  is below  $-3.74$  eV, the  $E_{form}$  of anaerobic NS- $TiO_2$  except the  $N_{Ti}S_{Ti}-TiO_2$  and  $N_{Ti}S_{Ti}-TiO_2$  are lower than zero, indicating that the corresponding doping processes all are exothermic reactions. In contrast, the doping processes of the  $N_{Ti}S_{Ti}-TiO_2$  and  $N_{Ti}S_{Ti}-TiO_2$  with positive  $E_{form}$  require the extra energy supplied by environment, which is more difficult to perform. With the  $\mu'_O$  moving forward higher chemical potential, the  $E_{form}$  of the anaerobic NS- $TiO_2$  gradually pass over zero point. As the  $\mu'_O$  is bigger than  $-2.46$  eV, the doping processes of all NS- $TiO_2$  with positive  $E_{form}$  become non-spontaneous reactions, implying that the O-rich condition inhibits the doping process of NS- $TiO_2$ . But considering the relatively lower  $E_{form}$  of  $N_{Ti}S_{Ti}-TiO_2$  and  $N_{O_i}S_{Ti}-TiO_2$  under  $\mu'_O$  from  $-2.46$  to  $0$  eV, it is still possible to synthesize the  $N_{Ti}S_{Ti}-TiO_2$  and  $N_{O_i}S_{Ti}-TiO_2$  by controlling the  $O_2$  pressure and supplying enough energy. The previous experiment indicated the NS- $TiO_2$  could be prepared by annealing in air (approximate O-rich condition), in which the structures of O–N–O and S–O–Ti linkage were detected by the XPS technology [47]. The

**Table 2**The  $E_v$ ,  $E_1$ ,  $E_2$ ,  $E_c$ ,  $E_g$  and  $E_{\max}$  for the pure and N–S codoped anatase  $\text{TiO}_2$ .

No.	Doped $\text{TiO}_2$	$E_v$ (eV)	$E_1$ (eV)	$E_2$ (eV)	$E_c$ (eV)	$E_g$ (eV)	$E_{\max}$ (eV)
(a)	Pure	5.81	5.81	7.93	7.93	2.12	2.12
(b)	$\text{N}_0\text{S}_0$	4.54	4.54	6.06	6.06	1.52	1.52
(c)	$\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$	3.54	4.29	5.56	5.93	2.39	1.27
(d)	$\text{N}_0\text{S}_{\text{Ti}}$	3.86	4.70	6.15	6.15	2.29	1.45
(e)	$\text{N}_0\text{S}_{\text{S}}$	4.43	5.52	6.37	6.37	1.94	0.85
(f)	$\text{N}_{\text{S}}\text{S}_0$	3.90	5.31	6.41	6.41	2.51	1.10

result is quite consistent with the analysis on geometry structure (see Fig. 2b and d). Hence, to further investigate the photocatalytic activities of NS– $\text{TiO}_2$ , the electronic properties of  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$ ,  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ ,  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ ,  $\text{N}_0\text{S}_{\text{S}}$ – $\text{TiO}_2$  and  $\text{N}_{\text{S}}\text{S}_0$ – $\text{TiO}_2$  are discussed in the next section.

### 3.3. Electronic properties

To clarify the origination of enhanced visible-light photocatalytic activity of NS– $\text{TiO}_2$ , the electronic properties of pure- $\text{TiO}_2$ ,  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$ ,  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ ,  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ ,  $\text{N}_0\text{S}_{\text{S}}$ – $\text{TiO}_2$  and  $\text{N}_{\text{S}}\text{S}_0$ – $\text{TiO}_2$  are calculated by DFT. The calculated band structures and projected density of states (PDOS) of the pure and NS– $\text{TiO}_2$  are plotted in Fig. 4. Based on the calculated band structures, the  $E_v$  (the energy for the top of valence band),  $E_1$  (the energy for the bottom of the maximum gap in band gap),  $E_2$  (the energy for the top of the maximum gap in band gap),  $E_c$  (the energy for the bottom of conduction band),  $E_g$  (the energy for the band gap) and  $E_{\max}$  (the energy for the maximum gap in band gap,  $E_{\max} = E_1 - E_2$ ) of the pure and NS– $\text{TiO}_2$  are listed in Table 2.

The calculated  $E_g$  of pure- $\text{TiO}_2$  is 2.12 eV, which is lower than the experimental value of 3.20 eV. The underestimation is originated from the known limitation of DFT. The conduction band of pure- $\text{TiO}_2$  (see Fig. 4a) is mainly constituted of Ti 3d states, while the valence band is composed of O 2p and Ti 3d states. For the  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$  (see Fig. 4b), the conduction band still consists of the Ti 3d state, while the  $\text{N}_0$  2p and  $\text{S}_0$  3p states appear in the top of valence band. Thus the valence band extends forward the conduction band and the  $E_g$  is sharply decreased to 1.52 eV. Because of no impurity state in the band gap, the  $E_{\max}$  is also 1.52 eV, which makes the absorption edge of  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$  shift to the visible region. Different with those in the  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$ , the  $\text{N}_{\text{Ti}}$  2s,  $\text{N}_{\text{Ti}}$  2p,  $\text{S}_{\text{Ti}}$  3s and  $\text{S}_{\text{Ti}}$  3p states in the  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  (see Fig. 4c) are delocalized above the top of valence band. Especially, the  $\text{N}_{\text{Ti}}$  2s and  $\text{S}_{\text{Ti}}$  3s states appear in the same energy region with the  $\text{N}_{\text{Ti}}$  2p and  $\text{S}_{\text{Ti}}$  3p state, respectively, implying the hybridization of  $\text{N}_{\text{Ti}}$  2s ( $\text{S}_{\text{Ti}}$  3s) and  $\text{N}_{\text{Ti}}$  2p ( $\text{S}_{\text{Ti}}$  3p) states. Besides, a level of  $\text{N}_{\text{Ti}}$  2p state is delocalized below the bottom of conduction band. As a result, the  $E_{\max}$  (1.27 eV) of  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  becomes smaller than that of  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$  though the  $E_g$  of  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  is increased to 2.39 eV, which greatly decreases the critical energy of photon required by transferring electron. Surprisingly, the distributing regulations of  $\text{N}_0$  2p,  $\text{S}_{\text{Ti}}$  3s and  $\text{S}_{\text{Ti}}$  3p states in the  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  (see Fig. 4d) are similar to those of the  $\text{N}_0$  2p state in  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$  and  $\text{S}_{\text{Ti}}$  3s and  $\text{S}_{\text{Ti}}$  3p states in  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ . This suggests that the  $\text{N}_0$  2p state tend to be localized in the top of valence band, which leads to the extending of valence band. However, the hybridizing level of  $\text{S}_{\text{Ti}}$  2s and  $\text{S}_{\text{Ti}}$  2p states prefers to be delocalized above the valence band of  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ , which is beneficial to the decrease of  $E_{\max}$ . Thus compared to the  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ , the  $E_g$  of  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  is reduced to 2.29 eV. But the  $E_{\max}$  of  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  rises to 1.72 eV, mainly originating from no impurity state below the conduction band in the  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ . Different with the impurity states in the  $\text{N}_0\text{S}_0$ – $\text{TiO}_2$ ,  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  and  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$ , the  $\text{S}_{\text{S}}$  3p state in  $\text{N}_0\text{S}_{\text{S}}$ – $\text{TiO}_2$  (see Fig. 4e) and partial  $\text{N}_{\text{S}}$  2p state in  $\text{N}_{\text{S}}\text{S}_0$ – $\text{TiO}_2$  (see Fig. 4f) go deep into the band gap. As a result, the  $E_{\max}$  of  $\text{N}_0\text{S}_{\text{S}}$ – $\text{TiO}_2$  and  $\text{N}_{\text{S}}\text{S}_0$ – $\text{TiO}_2$  are significantly decreased to 0.85 eV

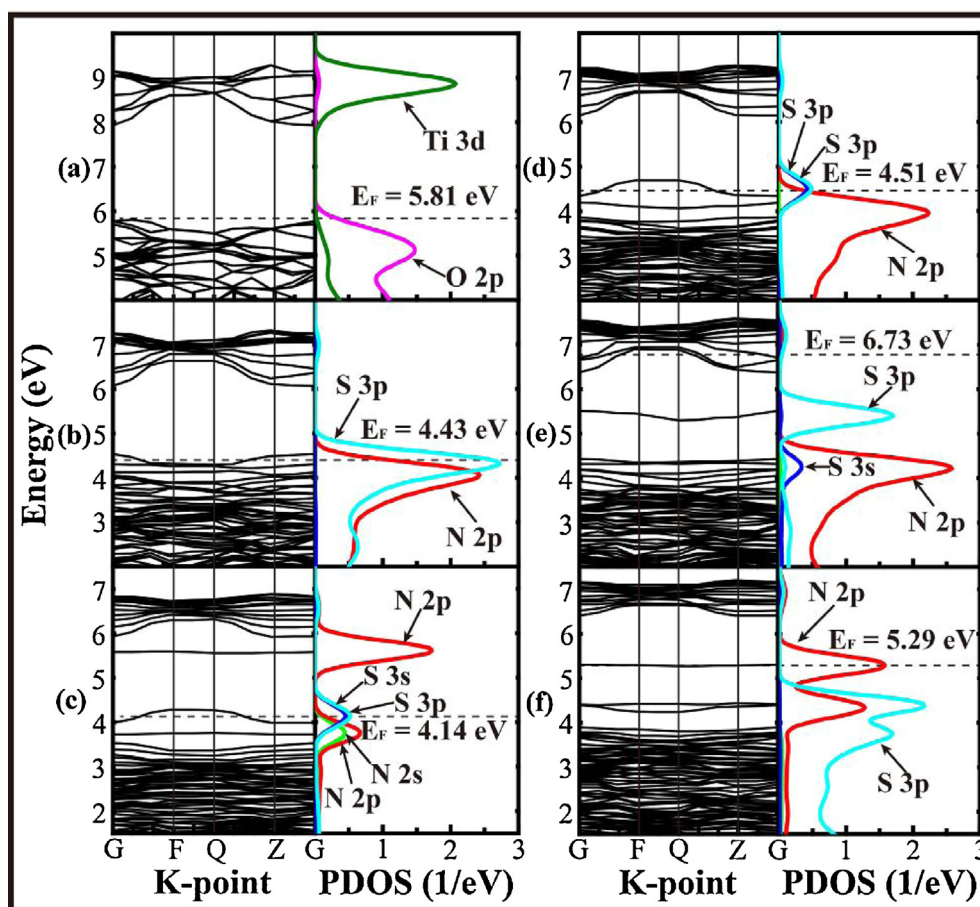
and 1.10 eV, respectively. Because of the N 2p and S 3s states localized in the top of valence band, the  $E_g$  of  $\text{N}_0\text{S}_{\text{S}}$ – $\text{TiO}_2$  is also reduced by 0.18 eV. In contrast, the  $E_g$  of  $\text{N}_{\text{S}}\text{S}_0$ – $\text{TiO}_2$  is decreased to 2.51 eV, mostly considered from the delocalization of N 2p and S 3p states. Therefore, the discussed impurity states all contributes to the red shift of NS– $\text{TiO}_2$ .

But according to many previous investigations, the visible-light photocatalytic activity is not only determined by the quantity of available photons, but also influenced by the quantum efficiency. The visible-light absorption of NS– $\text{TiO}_2$  only increases the quantity of available photons, but is not directly related to the quantum efficiency. However, it is much known that the recombination of photogenerated electron and hole easily occurs during the photocatalytic reaction and becomes the largest barrier for enhancing quantum efficiency. For the doped photocatalyst, many literatures discuss the impurity state delocalized in band gap as the recombination center of photogenerated electron and hole [60]. In contrast, other investigations also suggest that the impurity level in band gap is the separation center of photogenerated electron and hole [61,62]. But in fact, whether the impurity level is beneficial to enhancing quantum efficiency or not largely depends on the property of impurity level. During the photocatalytic reaction, the electron in the impurity level moves to the conduction band by capturing a photon with enough energy. Meanwhile a hole is left in the impurity level. Then the electron from the valence band can jump to the impurity level by capturing another appropriate photon, which means that the hole in the impurity level is eliminated and new hole forms in the top of valence band. As a result, the impurity level does not change, while an electron and a hole are generated in the valence band and conduction band, respectively, indicating the separation of photogenerated electron and hole. But this process is mainly determined by the mobility of photogenerated electron and hole, which can be indirectly characterized by the efficient masses (absolute value) of electron and hole. The smaller the efficient mass, the better the mobility. On the contrary, the larger efficient mass results in the worse mobility. The efficient masses of electron and hole are determined by the following formula:

$$m^* = \pm \frac{h/2\pi^2}{(d^2E/dk^2)^2} \quad (6)$$

where  $m^*$  is the efficient mass,  $h$  is the Planck constant,  $k$  is the wave vector and  $E$  is the energy of  $k$ . The positive and negative signs correspond to the electron and hole, respectively. It is clear that the electron and hole in the flat level with constant gradient have higher efficient masses, and contrarily those in bent level with variable gradient have lower efficient masses. In Fig. 4, compared to the levels of impurity states in other NS– $\text{TiO}_2$ , the hybridizing levels of S 3s and S 3p states in  $\text{N}_0\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  and  $\text{N}_0\text{S}_{\text{S}}$ – $\text{TiO}_2$  show the more obvious bend, indicating that the present levels are the efficient separation center of photogenerated electron and hole. However, the levels of N 2p state in  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$ – $\text{TiO}_2$  and  $\text{N}_{\text{S}}\text{S}_0$ – $\text{TiO}_2$  are approximate to straight line, corresponding to the recombination center of photogenerated electron and hole. Therefore, the shape and location of level of impurity state both are closely related to the photocatalytic activity of NS– $\text{TiO}_2$ .

Furthermore, according to the  $E_v$  and  $E_c$  in Table 2, it can be clearly seen that the valence and conduction bands of NS– $\text{TiO}_2$  both move down to the lower energy region. The  $E_v$  and  $E_c$  are decreased by more than 1.20 eV. It is easy to understand that the electron from donor (such as organic pollutant and  $\text{OH}^-$ ) is easier to jump to the lower energy level and combine with the photogenerated hole. Similarly, the photogenerated electron in the conduction band is also easier to shift to the empty energy level of acceptor (such as  $\text{O}_2$ ). In other words, the photogenerated hole in the lower energy level and the photogenerated electron in the higher energy level have



**Fig. 4.** Band structures and projected density of state (PDOS) plots for pure and N–S codoped TiO<sub>2</sub>: (a) pure-TiO<sub>2</sub>, (b) N<sub>0</sub>S<sub>0</sub>–TiO<sub>2</sub>, (c) N<sub>11</sub>S<sub>11</sub>–TiO<sub>2</sub>, (d) N<sub>0</sub>S<sub>1</sub>–TiO<sub>2</sub>, (e) N<sub>0</sub>S<sub>1</sub>–TiO<sub>2</sub> and (f) N<sub>1</sub>S<sub>0</sub>–TiO<sub>2</sub>. To compare relative energies of band structures and PDOS for different N–S codoped TiO<sub>2</sub>, all energies are raised by the corresponding  $E_F$ . The dashed lines stand for the Fermi level. The magenta lines represent the PDOS of O 2p, olive for Ti 3d, green for N 2s, red for N 2p, blue for S 3s and cyan for S 3p (For interpretation of the references to color in this figure legend, the reader is referred to the web version of the article.).

the stronger oxidizability and reducibility, respectively. Therefore, the oxidizability of photogenerated hole in the top of valence band is enhanced and the reducibility of photogenerated electron in the bottom of conduction band is weakened in the NS–TiO<sub>2</sub>. According to many previous investigations on the mechanism of photocatalytic degradation, it is widely confirmed that the O<sub>2</sub> on the surface of TiO<sub>2</sub> can be reduced into •O<sub>2</sub><sup>−</sup> ion by capturing a photogenerated electron from the conduction band. In contrast, the hydroxyl group (−OH) on the surface of TiO<sub>2</sub> can be oxidized into •OH radical by capturing a photogenerated hole from the valence band. In addition, the photogenerated hole also can be directly captured by the organic pollutant. These •O<sub>2</sub><sup>−</sup> ion, •OH radical and hole all are crucial oxidants in the degradation of organic pollutant. As a result, the NS–TiO<sub>2</sub> prefers to generate more •OH radicals, rather than •O<sub>2</sub><sup>−</sup> ions. Moreover, for different organic pollutants and photocatalysts, the contributions of •O<sub>2</sub><sup>−</sup> ion, •OH radical and hole are also different. Our recent study on the degradation of Rhodamine B (RhB) with B–C codoped anatase TiO<sub>2</sub> indicates that the •OH radical plays the domain role in the photocatalytic reaction. This is because the location of the valence band edges ( $E_v$ ) of B–C codoped anatase TiO<sub>2</sub> is lower than the normal potential of the OH<sup>−</sup>/•OH couple [61–63]. However, another investigation on the degradation of methyl orange (MO) with BiOI confirms that the hole is the main oxidant. This is due to the valence band edges ( $E_v$ ) of BiOI is higher than the OH<sup>−</sup>/•OH couple potential [64]. Hence, the energy values in the top of valence band and bottom of conduction band

have a significant influence on the mechanism of photocatalytic reaction.

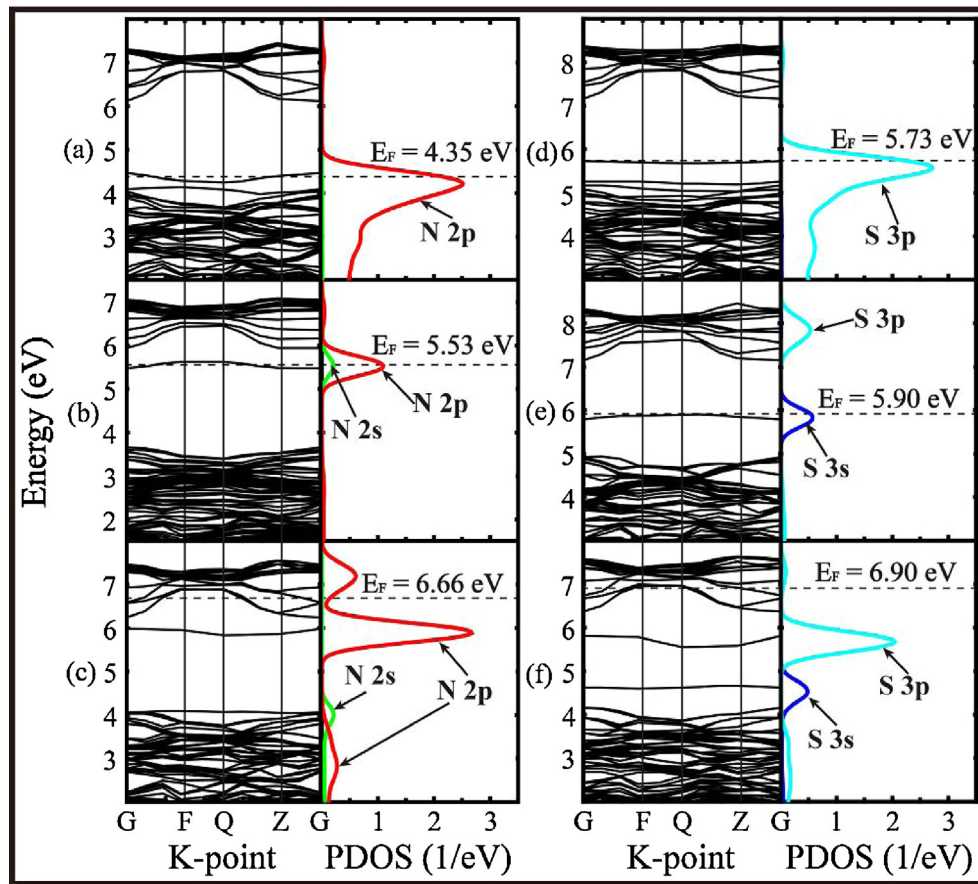
Considering the variation of Fermi levels in the NS–TiO<sub>2</sub>, the further investigation is done. The  $E_F$  in pure anatase TiO<sub>2</sub> is 5.81 eV, while the  $E_F$  in NS–TiO<sub>2</sub> ranges from 4.14 (N<sub>11</sub>S<sub>11</sub>–TiO<sub>2</sub>) to 6.73 eV (N<sub>0</sub>S<sub>1</sub>–TiO<sub>2</sub>). Besides, because of the moving of valence band and conduction band, the distance between the Fermi level and the valence band (conduction band) also exhibits different change. The shift of Fermi level implies the redistribution of charges after doping N and S atoms into the lattice of TiO<sub>2</sub>. To investigate the origination of shift of Fermi level, the Mulliken populations of NS–TiO<sub>2</sub> are calculated (see Table 3). In pure anatase TiO<sub>2</sub>, the Mulliken populations of O and Ti atoms are −0.67 and 1.33, respectively. Besides, as a typical semiconductor, the Fermi level of pure-TiO<sub>2</sub> is in the top of valence band. But in the N<sub>0</sub>S<sub>0</sub>–TiO<sub>2</sub>, the Mulliken populations of Ti atoms bonded to N<sub>0</sub> and S<sub>0</sub> atoms are lower than 1.33 because

**Table 3**

The  $E_v$ ,  $E_1$ ,  $E_2$ ,  $E_c$ ,  $E_g$  and  $E_{max}$  for the N- and S-doped anatase TiO<sub>2</sub>.

No.	Doped TiO <sub>2</sub>	$E_v$ (eV)	$E_1$ (eV)	$E_2$ (eV)	$E_c$ (eV)	$E_g$ (eV)	$E_{max}$ (eV)
(a)	N <sub>0</sub>	4.46	4.46	6.12	6.12	1.66	1.66
(b)	N <sub>11</sub>	3.65	3.65	5.48	5.94	2.29	1.83
(c)	N <sub>1</sub>	4.09	4.09	5.83	6.25	2.16	1.74
(d)	S <sub>0</sub>	5.26	5.73	7.16	7.16	1.90	1.43
(e)	S <sub>11</sub>	4.92	5.90	7.15	7.15	2.23	1.25
(f)	S <sub>1</sub>	4.16	4.67	5.55	6.37	2.21	0.88





**Fig. 5.** Band structures and PDOS plots for N- and S-doped anatase  $\text{TiO}_2$ : (a)  $\text{N}_0\text{-TiO}_2$ , (b)  $\text{N}_{\text{Ti}}\text{-TiO}_2$ , (c)  $\text{N}_{\text{i}}\text{-TiO}_2$ , (d)  $\text{S}_0\text{-TiO}_2$ , (e)  $\text{S}_{\text{Ti}}\text{-TiO}_2$  and (f)  $\text{S}_{\text{i}}\text{-TiO}_2$ . Other refers to Fig. 4.

the electronegativity of N and S atoms is smaller than that of O atom. However, the Mulliken population of  $\text{N}_0$  atom is larger than that of O atom in pure- $\text{TiO}_2$ , due to the fact that the  $\text{N}_0\text{-Ti}$  bond is shorter than  $\text{O-Ti}$  bond (see Table 1). As a result, the adjacent Ti atoms prefer to be close to the  $\text{N}_0$  atom rather than O atom. Meanwhile, the interaction between O and Ti atoms is also weakened. This explains why the Mulliken populations of Ti atoms bonded to  $\text{N}_0$  atom are decreased, while the Mulliken population of  $\text{N}_0$  atom rises. As for  $\text{S}_0$  atom, the Mulliken population of  $\text{S}_0$  atom is only

−0.21 because of its weak electronegativity. This is well consistent with the fact that the Fermi level is nearly above the  $\text{N}_0$  2p state and in the middle of  $\text{S}_0$  3p state (see Fig. 4b), indicating that the level of  $\text{N}_0$  2p state is filled with electrons and that of  $\text{S}_0$  3p state is half filled. However, the Fermi levels in the  $\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}\text{-TiO}_2$  and  $\text{N}_0\text{S}_{\text{Ti}}\text{-TiO}_2$  both are delocalized in the band gap, approaching to the middle of hybridizing levels of  $\text{S}_{\text{Ti}}$  3s and  $\text{S}_{\text{Ti}}$  3p states. This indicates that the hybridizing levels of  $\text{S}_{\text{Ti}}$  3s and  $\text{S}_{\text{Ti}}$  3p states are also half filled. The previous analysis on the efficient mass indicates that the

**Table 4**

Mulliken populations on the impurity and adjacent matrix atoms in the supercells of N–S codoped anatase  $\text{TiO}_2$ .

Doped $\text{TiO}_2$ <sup>a</sup>	N population	S population	O population		Ti population	
			Bonded to N	Bonded to S	Bonded to N	Bonded to S
$\text{N}_0\text{S}_0$	−0.69	−0.21			1.28 <sub>eq</sub> (2) <sup>b</sup> 1.30 <sub>ax</sub>	1.18 <sub>eq</sub> (2) 1.25 <sub>ax</sub>
$\text{N}_{\text{Ti}}\text{S}_{\text{Ti}}$	0.25	1.79	−0.39 <sub>eq</sub> −0.40 <sub>ax</sub>	−0.80 <sub>eq</sub> −0.82 <sub>eq</sub> −0.76 <sub>ax</sub>		
$\text{N}_0\text{S}_{\text{Ti}}$	−0.69	1.77		−0.80 <sub>eq</sub> −0.82 <sub>eq</sub> −0.77 <sub>ax</sub>	1.27 <sub>eq</sub> 1.28 <sub>eq</sub> 1.28 <sub>ax</sub>	
$\text{N}_0\text{S}_{\text{i}}$	−0.69	0.67		−0.71 −0.73	1.25 <sub>eq</sub> 1.27 <sub>eq</sub> 1.26 <sub>ax</sub>	
$\text{N}_{\text{i}}\text{S}_0$	−0.25	−0.37	−0.37		1.25 1.26	1.13 <sub>eq</sub> 1.18 <sub>eq</sub> 1.18 <sub>ax</sub>

<sup>a</sup> In the pure anatase  $\text{TiO}_2$ : O population = −0.67, Ti population = 1.33.

<sup>b</sup> The numbers in the parentheses describes the quantity of atoms with same Mulliken population.

hybridizing levels of  $S_{Ti}$  3s and  $S_{Ti}$  3p states are the efficient separation center of photogenerated electron and hole. As a result, not only can the electrons in the present levels directly jump to the conduction bands, but also the electrons in the valence bands can jump to the present levels. But the hybridizing level of  $N_{Ti}$  2s and  $N_{Ti}$  2p states in  $N_{Ti}S_{Ti}-TiO_2$  are filled, owing to the Mulliken population (0.25) of  $N_{Ti}$  atom smaller than that (1.79) of  $S_{Ti}$  atom. Similar to that in  $N_0S_0-TiO_2$ , the level of  $N_0$  2p state in  $N_0S_{Ti}-TiO_2$  is also filled. However, in  $N_0S_i-TiO_2$ , the Fermi level enters the bottom of conduction band, indicating that the  $N_0S_i-TiO_2$  has the metal-like electroconductivity and the  $Ti^{3+}$  ion exists in the present  $TiO_2$ . This is due to the fact that the  $S_i$  atom is bonded to O atoms (see Fig. 2i) and shows the positive Mulliken population (0.67), which weakens adjacent O–Ti bonds and decreases the quantity of electrons transferring from Ti atoms to O atoms. Therefore, compared to those in pure- $TiO_2$ , the more levels of Ti 3d state in  $N_0S_i-TiO_2$  are occupied. The modified electroconductivity of  $N_0S_i-TiO_2$  are in favor of the transferring of photogenerated electron, which improves the separating rate of photogenerated electron and hole. Though in  $N_iS_0-TiO_2$  the interstitial atom (N) is also introduced, the  $N_i$  atom is simultaneously bonded to Ti and O atom and shows negative Mulliken population (–0.25). Besides, the Mulliken population of O atom bonded to  $N_i$  atom is decreased to –0.37. Thus the Fermi level is delocalized in the level of  $N_i$  2p state, indicating that the present level is half filled. However, the previous analysis shows that the efficient mass of electron in the present level is greater than that in other levels. Therefore the electron in present level cannot easily transfer to the conduction band. Besides, the electron from the valence band or other impurity levels can be trapped in the present level, which inhibits the transferring of electron.

Another phenomenon should be noted that the distributions of  $S_0$  3p states in the  $N_0S_0-TiO_2$  (see Fig. 4b) and  $N_iS_0-TiO_2$  (see Fig. 4f) are different though the S atoms both are doped in the positions of O atoms. Hence, the impurity level of S atom is influenced by N atom, indicating that the band structure of NS- $TiO_2$  is not mechanical mixture of the band structures of N- $TiO_2$  and S- $TiO_2$ . Thus, to explore the interaction between N and S atoms, the N- $TiO_2$  ( $N_0-TiO_2$ ,  $N_{Ti}-TiO_2$  and  $N_i-TiO_2$ ) and S-doped  $TiO_2$  ( $S_0-TiO_2$ ,  $S_{Ti}-TiO_2$  and  $S_i-TiO_2$ ) are also investigated. The calculated band structure and PDOS are shown in Fig. 5. In addition, the  $E_v$ ,  $E_1$ ,  $E_2$ ,  $E_c$ ,  $E_g$  and  $E_{max}$  are also calculated (see Table 4). It can be seen clearly that the level of  $N_0$  2p state in the  $N_0-TiO_2$  (see Fig. 5a) and the level of  $S_0$  3p state in the  $S_0-TiO_2$  (see Fig. 5d) both tend to be delocalized above the valence band, different with those in the  $N_0S_0-TiO_2$ . As a result, the  $E_g$  of  $N_0-TiO_2$  (1.66 eV) and  $S_0-TiO_2$  (1.90 eV) are larger than that of  $N_0S_0-TiO_2$ . Besides, the Fermi levels are delocalized in the levels of N 2p and S 3p states, indicating that the levels of N 2p and S 3p states are mostly filled. In the  $N_{Ti}-TiO_2$  (see Fig. 5b), the N 2s state hybridizes with N 2p state, similar to that in the  $N_{Ti}S_{Ti}-TiO_2$ . However, the hybridizing level of  $N_{Ti}$  2s and  $N_{Ti}$  2p states is close to the bottom of conduction band. Besides, the single  $N_{Ti}$  2p state is not found in the band gap. In  $S_{Ti}-TiO_2$  (see Fig. 5e), the S 3s and S 3p states are in different energy region. Especially, the S 3p state is localized in the conduction band. As a result, though the  $E_g$  of  $N_{Ti}-TiO_2$  (2.29 eV) and  $S_{Ti}-TiO_2$  (2.23 eV) are larger than that (2.12 eV) of pure- $TiO_2$ , the  $E_{max}$  of  $N_{Ti}-TiO_2$  (1.83 eV) and  $S_{Ti}-TiO_2$  (1.25 eV) are smaller than 2.12 eV because of the delocalized levels. In the  $N_i-TiO_2$  (see Fig. 5c) and  $S_i-TiO_2$  (see Fig. 5f), the  $N_i$  2p,  $S_i$  3s and  $S_i$  3p states are mainly delocalized in the band gap, while the  $N_i$  2s state in  $N_i-TiO_2$  is localized in the top of valence band. This results in that the  $E_g$  of  $N_i-TiO_2$  (2.16 eV) and  $S_i-TiO_2$  (2.21 eV) is slightly larger than that of pure- $TiO_2$  (2.12 eV), but the  $E_{max}$  of  $N_i-TiO_2$  and  $S_i-TiO_2$  are decreased to 1.74 and 0.88 eV, respectively. In addition, the Fermi levels of  $N_i-TiO_2$  and  $S_i-TiO_2$  both enter the conduction bands. Though in the  $N_iS_0-TiO_2$  the Fermi level is also in the conduction band, the

Fermi level in the  $N_0S_i-TiO_2$  is only close to the middle of band gap, implying that the behavior of  $N_i$  atom is changed by  $S_0$  atom. Meanwhile, the  $S_0$  atom is also influenced by the  $N_i$  atom. Hence, the synergistic effects of N and S atoms make the NS- $TiO_2$  exhibit different electronic properties with those of N- $TiO_2$  and S- $TiO_2$ . But the NS- $TiO_2$  also inherits partial electronic property of N- $TiO_2$  and S- $TiO_2$ . This is beneficial to synthesizing the NS- $TiO_2$  with expected electronic property.

#### 4. Conclusions

The visible-light photocatalytic activity of NS- $TiO_2$  is studied by the first-principles. The NS- $TiO_2$  except  $N_{Ti}S_{Ti}-TiO_2$  is the anaerobic doped system, which enjoys the O-poor growth condition. In the O-poor condition, the  $N_0S_0-TiO_2$ ,  $N_0S_i-TiO_2$  and  $N_iS_0-TiO_2$  are the most stable doped system. However, with increasing the  $\mu_O$ , the  $N_0S_{Ti}-TiO_2$  and  $N_{Ti}S_{Ti}-TiO_2$  successively become the most stable doped system. But the doping processes of  $N_0S_{Ti}-TiO_2$  and  $N_{Ti}S_{Ti}-TiO_2$  require extra energy. The photocatalytic activities of  $N_0S_0-TiO_2$ ,  $N_{Ti}S_{Ti}-TiO_2$ ,  $N_0S_{Ti}-TiO_2$ ,  $N_0S_i-TiO_2$  and  $N_iS_0-TiO_2$  are determined not only by the values of energy gaps ( $E_g$ ) and distributions of impurity states, but also depend on the properties of impurity states and the locations of Fermi levels. The impurity state localized in the valence band reduces the  $E_g$  and that delocalized in the band gap decreases the  $E_{max}$ , which both enhance the absorptions of visible light. But the separating efficiency of photogenerated electron and hole is controlled by the property of impurity level. In the  $N_{Ti}S_{Ti}-TiO_2$  and  $N_0S_{Ti}-TiO_2$ , the hybridizing levels of  $S_{Ti}$  3s and  $S_{Ti}$  3p states are the effective separation center of photogenerated electron and hole, in which the photogenerated electron and hole have smaller efficient masses. In contrast, the level of  $N_{Ti}$  2p state (close to the conduction band) in  $N_{Ti}S_{Ti}-TiO_2$  and level of  $N_i$  2p state (close to the middle of band gap) in  $N_iS_0-TiO_2$  easily become the combination or trap center of photogenerated electron and hole. The  $N_0S_i-TiO_2$  with Fermi level in the conduction band shows the best electroconductivity, which improves the ability of transferring electron. Furthermore, the valence band and conduction band of NS- $TiO_2$  move toward the lower energy region compared to those of pure- $TiO_2$ , which enhances the oxidizability of photogenerated hole in the top of valence band but weakens the reducibility of photogenerated electron in the bottom of conduction band. This contributes to forming more  $\bullet OH$  radical than  $\bullet O_2^-$  ion during the photocatalytic reaction. In addition, the NS- $TiO_2$  not only exhibits many same electronic properties with N- $TiO_2$  and S- $TiO_2$ , but also produces many new electronic properties, implying that the electronic property of NS- $TiO_2$  does not mechanically consist of those of N- $TiO_2$  and S- $TiO_2$ . This investigation will provide some new insights into designing and synthesizing the codoped or multidoped  $TiO_2$  system with expected electronic property by adjusting the growth condition.

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#### References

- [1] A. Fujishima, K. Honda, *Nature* 238 (1972) 37.
- [2] Y. Xu, M.A.A. Schoonen, *American Mineralogist* 85 (2000) 543.



- [3] Q.J. Xiang, J.G. Yu, M. Jaroniec, *Chemical Society Reviews* 41 (2012) 782.
- [4] M. Anpo, H. Yamashita, Y. Ishihashi, Y. Fujii, M. Honda, *Journal of Physical Chemistry* 101 (1997) 2632.
- [5] P. Madhusudan, J.R. Ran, J. Zhang, J.G. Yu, G. Liu, *Applied Catalysis B* 110 (2011) 286.
- [6] X.X. Yu, S.W. Liu, J.G. Yu, *Applied Catalysis B* 104 (2011) 12.
- [7] W.G. Wang, J.G. Yu, Q.J. Xiang, B. Cheng, *Applied Catalysis B* 119–120 (2012) 109.
- [8] T. Inoue, A. Fujishima, S. Konishi, K. Honda, *Nature* 277 (1979) 637.
- [9] I. Laueremann, D. Meissner, R. Memming, *Journal of Electroanalytical Chemistry* 228 (1987) 45.
- [10] J. Zhang, J.G. Yu, Y.M. Zhang, Q. Li, J.R. Gong, *Nano Letters* 11 (2011) 4774.
- [11] Q.J. Xiang, J.G. Yu, M. Jaroniec, *Journal of the American Ceramic Society* 134 (2012) 6575.
- [12] J. Zhang, J.G. Yu, M. Jaroniec, J.R. Gong, *Nano Letters* 12 (2012) 4584.
- [13] S.W. Liu, J.G. Yu, M. Jaroniec, *Journal of the American Ceramic Society* 132 (2010) 11914.
- [14] J.G. Yu, Y.R. Su, B. Cheng, *Advanced Functional Materials* 17 (2007) 1984.
- [15] J.G. Yu, G.P. Dai, B.B. Huang, *Journal of Physical Chemistry C* 113 (2009) 16394.
- [16] Q.J. Xiang, J.G. Yu, W.G. Wang, M. Jaroniec, *Chemical Communications* 47 (2011) 6906.
- [17] X.N. Lu, B.Z. Tian, F. Chen, J.L. Zhang, *Thin Solid Films* 519 (2010) 111.
- [18] Y. Park, W. Kim, H. Park, T. Tachikawa, T. Majima, W. Choi, *Applied Catalysis B* 91 (2009) 355.
- [19] R. Asahi, T. Morikawa, T. Ohwaki, K. Aoki, Y. Taga, *Science* 293 (2001) 269.
- [20] J.C. Yu, J.G. Yu, W.K. Ho, Z.T. Jiang, L.Z. Zhang, *Chemistry of Materials* 14 (2002) 3808.
- [21] S.W. Liu, J.G. Yu, W.G. Wang, *Physical Chemistry Chemical Physics* 12 (2010) 12308.
- [22] G.D. Yang, Z.F. Yan, T.C. Xiao, *Applied Surface Science* 258 (2012) 4016.
- [23] M. Sathish, B. Viswanathan, R.P. Viswanath, C.S. Gopinath, *Chemistry of Materials* 17 (2005) 6349.
- [24] F.F. Li, Y.S. Jiang, M.S. Xia, M.M. Sun, B. Xue, D.R. Liu, X.G. Zhang, *Journal of Physical Chemistry C* 113 (2009) 18134.
- [25] X.H. Tang, D.Y. Li, *Journal of Physical Chemistry C* 112 (2008) 5405.
- [26] R. Plass, S. Pelet, J. Krueger, M. Gratzel, U. Bach, *Journal of Physical Chemistry B* 106 (2002) 7578.
- [27] S.G. Hickey, D.J. Riley, E.J. Tull, *Journal of Physical Chemistry B* 104 (2000) 7623.
- [28] I. Robel, M. Kuno, P.V. Kamat, *Journal of the American Ceramic Society* 129 (2007) 4136.
- [29] I. Robel, V. Subramanian, M. Kuno, P.V. Kamat, *Journal of the American Ceramic Society* 128 (2006) 2385.
- [30] W.T. Sun, Y. Yu, H.Y. Pan, X.F. Gao, Q. Chen, L.M. Peng, *Journal of the American Ceramic Society* 130 (2008) 1124.
- [31] L.F. Qi, J.G. Yu, M. Jaroniec, *Physical Chemistry Chemical Physics* 13 (2011) 8915.
- [32] Y. Wang, C. Feng, M. Zhang, J.J. Yang, Z.J. Zhang, *Applied Catalysis B* 100 (2010) 84.
- [33] G. Barolo, S. Livraghi, M. Chiesa, M.C. Paganini, E. Giamello, *Journal of Physical Chemistry C* 116 (2012) 20887.
- [34] D.D. Camillo, F. Ruggieri, S. Santucci, L. Lozz, *Journal of Physical Chemistry C* 116 (2012) 18427.
- [35] J. Wang, D.N. Tafen, J.P. Lewis, Z.L. Hong, A. Manivannan, M. Zhi, M. Li, N.Q. Wu, *Journal of the American Ceramic Society* 131 (2009) 12290.
- [36] S.H. Nam, T.K. Kim, J.H. Boo, *Catalysis Today* 185 (2012) 259.
- [37] H.X. Li, X.Y. Zhang, Y.N. Huo, J. Zhu, *Environmental Science and Technology* 41 (2007) 4410.
- [38] Y. Cong, J.L. Zhang, F. Chen, M. Anpo, *Journal of Physical Chemistry C* 111 (2007) 6976.
- [39] T. Tachikawa, Y. Takai, S. Tojo, M. Fujitsuka, H. Irie, K. Hashimoto, T. Majima, *Journal of Physical Chemistry B* 110 (2006) 13158.
- [40] X.B. Chen, C. Burda, *Journal of the American Ceramic Society* 130 (2008) 5018.
- [41] F.H. Tian, C.B. Liu, *Journal of Physical Chemistry B* 110 (2006) 17866.
- [42] Z.S. Lin, A. Orlov, R.M. Lambert, M.C. Payne, *Journal of Physical Chemistry B* 109 (2005) 20948.
- [43] Y. Cui, H. Du, L.S. Wen, *Solid State Communications* 149 (2009) 634.
- [44] K.S. Yang, Y. Dai, B.B. Huang, *Journal of Physical Chemistry C* 111 (2007) 12086.
- [45] K.S. Yang, Y. Dai, B.B. Huang, *Journal of Physical Chemistry C* 111 (2007) 18985.
- [46] J.A. Rengifo-Herrera, K. Pierzchała, A. Sienkiewicz, L. Forro, J. Kiwi, C. Pulgarin, *Applied Catalysis B* 88 (2009) 398.
- [47] J.A. Rengifo-Herrera, E. Mielczarski, J. Mielczarski, N.C. Castillo, J. Kiwi, C. Pulgarin, *Applied Catalysis B* 84 (2008) 448.
- [48] K.M. Parida, N. Sahu, A.K. Tripathi, V.S. Kamble, *Environmental Science and Technology* 44 (2010) 4155.
- [49] M. Ksibi, S. Rossignol, J.M. Tatibouët, C. Trapalis, *Materials Letters* 62 (2008) 4204.
- [50] J.A. Rengifo-Herrera, C. Pulgarin, *Solar Energy* 84 (2010) 37.
- [51] G.T. Yan, M. Zhang, J. Hou, J.J. Yang, *Materials Chemistry and Physics* 129 (2011) 553.
- [52] M. Behpour, V. Atouf, *Applied Surface Science* 258 (2012) 6595.
- [53] Q.J. Xiang, J.G. Yu, M. Jaroniec, *Physical Chemistry Chemical Physics* 13 (2011) 4853.
- [54] M.D. Segall, P.L.D. Lindan, M.J. Probert, C.J. Pickard, P.J. Hasnip, S.J. Clark, M.C. Payne, *Journal of Physics-Condensed Matter* 14 (2002) 2717.
- [55] J.P. Perdew, K. Burk, M. Ernzerhof, *Physical Review Letters* 77 (1996) 3865.
- [56] J.P. Perdew, Y. Wang, *Physical Review B* 45 (1992) 13244.
- [57] H.J. Monkhorst, J.D. Pack, *Physical Review B* 13 (1976) 5188.
- [58] R. Long, N.J. English, *Journal of Physical Chemistry C* 113 (2009) 8373.
- [59] C.D. Valentin, E. Finazzi, G. Pacchioni, *Chemistry of Materials* 20 (2008) 3706.
- [60] Z.H. Xu, J.G. Yu, *Nanoscale* 3 (2011) 3138.
- [61] J.G. Yu, Q. Li, S.W. Liu, M. Jaroniec, *Chemistry-A European Journal* 19 (2013) 2433.
- [62] J.G. Yu, P. Zhou, Q. Li, *Physical Chemistry Chemical Physics* (2013), <http://dx.doi.org/10.1039/C3CP44651D>.
- [63] X.X. Yu, J.G. Yu, B. Cheng, B.B. Huang, *Chemistry-A European Journal* 15 (2009) 6731.
- [64] Y.N. Wang, K.J. Deng, L.Z. Zhang, *Journal of Physical Chemistry C* 115 (2011) 14300.